

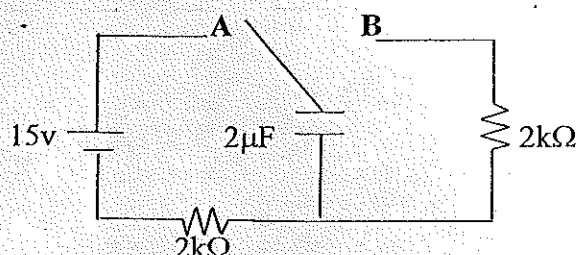
# RC circuits extended

1. When the switch is in position A, the circuit reaches steady state conditions. It is then thrown to position B.
  - a. Is the capacitor charging or discharging?
  - b. What is the time constant?
  - c. Find the capacitor voltage as a function of time.
  - d. Find the resistor voltage as a function of time.
  - e. Find the current as a function of time.
  - f. At 0.25 ms, what is the voltage and current across the resistor and the voltage across the capacitor?

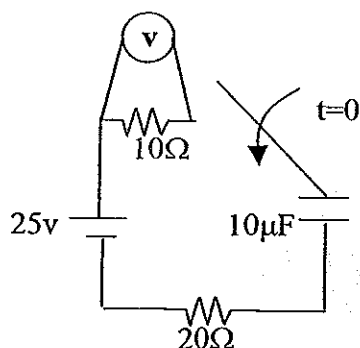
$$\tau = RC = 2k\Omega \times 2\mu F = 4ms$$

$$V = V_0 e^{-t/\tau} = 15V e^{-t/4ms}$$

$$i = \frac{V}{R} = \frac{15V}{2k\Omega} e^{-t/4ms} = 7.5mA e^{-t/4ms}$$



2. The circuit is in steady state at  $t = 0^-$  (switch is originally open).
  - a. What is the voltmeter reading at this point?
 Just as the switch is closed:
  - b. Determine the voltmeter reading.
  - c. Determine the current as a function of time.
  - d. Find the voltmeter reading at 0.5 ms.
 After the circuit again reaches steady state:
  - e. Determine the voltmeter reading.
  - f. Write a differential equation using variables (use Kirchhoff's voltage loop rule).



1. a) Discharging

$$b) \tau = RC = (2k)(2\mu F) = 0.004s = 4ms \quad (45-35)$$

c)

$$V_C = 15e^{-250t}$$

$$d) V_R = -15e^{-250t}$$

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$$e) i(t) = 7.0075e^{-250t}$$

$$f) V_C = V_R = 14.09V$$

$$i_R = 1.0075A_{avg}$$

2. a)  $V=0$ 

$$b) \frac{25}{30} = .83A \Rightarrow V = iR = 8.3V$$

$$25 = 30A$$

$$V_C(0^-) = V_C(0^+)$$

$$c) i = .83e^{-t/35.4}$$

$$R_C = 30\Omega$$

$$i = .83e^{-3333.3t}$$

$$C = 10\mu F$$

$$\tau = RC = 35.4$$



$$d) V = (.83)(10)e^{-3333.3(15 \times 10^{-3})}$$

e)  $V=0$ 

$$V = 1.57 \text{ volts}$$

f)

$$-25 + 10i_1 + V_C + 20i_2 = 0$$

$$30A + \frac{q}{C} = 25$$

$$30 \frac{dq}{dt} + \frac{q}{C} = 25$$

3. a)

$$R_{eq} = 20\Omega$$

$$a) \therefore I = \frac{25}{20} = 1.25A$$

$$b) (10)(1.25) = 12.5V$$

$$b) V_c = 25 - 12.5V = 12.5V$$

c)

$$V_c = 12.5e^{-t/47}$$

$$R_{eq} = 10\Omega$$

$$\tau = R_{eq} = (4.7)(10) = 47s$$

$$V_c = 12.5e^{-t/47}$$

$$\therefore V = \frac{1}{2} V_c \text{ because of 2-50V resistors}$$

$$V = 6.25e^{-t/47} \text{ Volts}$$

$$d) V = 6.25e^{-t/47}$$

$$V = 5.99 \text{ Volts}$$

(3)

Answer without 12  $\Omega$ 

4. a)



$$\frac{3}{12} \parallel \frac{1}{12} = \frac{4}{12} = 3\Omega$$

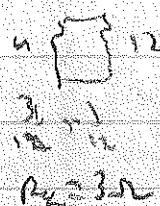


$$R_{eq} = 11\Omega$$

$$\frac{20}{11\Omega} = 1.82 \text{ Amps}$$

$$\therefore V_{Ra} = (1.82)(8) = 14.5\text{V}$$

$$\therefore V_c = 20 - 14.5 = 5.5\text{V} \quad (5.5\text{V})$$



b)

$$V_1 = V_c = 5.5e^{-t/RC}$$

$$\tau = RC = (3)(3) = 9$$

$$V_1 = 5.5e^{-t/9} \text{ V}$$

$$V_2 = \left(\frac{10}{10+2}\right)(5.5e^{-t/9})$$

$$V_3 = \left(\frac{2}{10+2}\right)(5.5e^{-t/9})$$

$$\underline{V_2 = 4.58e^{-t/9} \text{ V}}$$

$$\underline{V_3 = .92e^{-t/9} \text{ V}}$$